

Linear Programming Worksheet

Algebra 2

1. The area of a parking lot is 600 square meters. A car requires 6 square meters. A bus requires 30 square meters. The attendant can handle only 60 vehicles. If a car is charged \$2.50 and a bus \$7.50, how many of each should be accepted to maximize income?

Constraints:

$$c \geq 0; b \geq 0$$

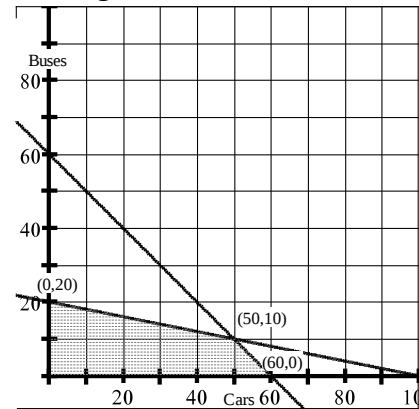
$$c + b \leq 60$$

$$6c + 30b \leq 600$$

Profit:

$$P(c, b) = 2.5c + 7.5b$$

	Car (c)	Bus (b)	Combined
Area:	6	30	600
Quantity:			60
\$:	\$2.50	\$7.50	



Answer: 50 cars and 10 buses

2. The B & W Leather Company wants to add handmade belts and wallets to its product line. Each belt nets the company \$18 in profit, and each wallet nets \$12. Both belts and wallets require cutting and sewing. Belts require 2 hours of cutting time and 6 hours of sewing time. Wallets require 3 hours of cutting time and 3 hours of sewing time. If the cutting machine is available 12 hours a week and the sewing machine is available 18 hours per week, what ratio of belts and wallets will produce the most profit within the constraints?

Constraints:

$$b \geq 0; w \geq 0$$

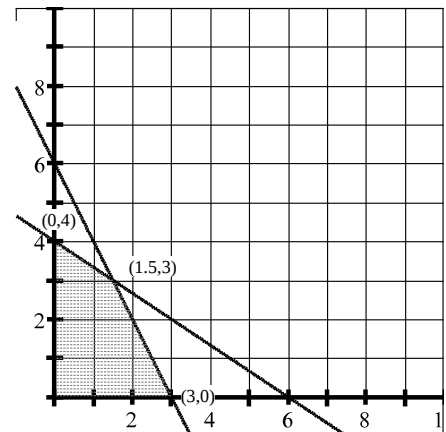
Cutting: $2b + 3w \leq 12$

Sewing: $6b + 3w \leq 18$

	Belts (b)	Wallets (w)	Combined
Cutting:	2	3	12
Sewing:	6	3	18
\$:	\$18	\$12	

Profit:

$$P(b, w) = 18b + 12w$$



Answer: 1.5 belts to 3 wallets

3. Toys-A-Go makes toys at Plant A and Plant B. Plant A needs to make a minimum of 1000 toy dump trucks and fire engines. Plant B needs to make a minimum of 800 toy dump trucks and fire engines. Plant A can make 10 toy dump trucks and 5 toy fire engines per hour. Plant B can produce 5 toy dump trucks and 15 toy fire engines per hour. It costs \$30 per hour to produce toy dump trucks and \$35 per hour to operate produce toy fire engines. How many hours should be spent on each toy in order to minimize cost? What is the minimum cost?

Constraints:

$$d \geq 0; f \geq 0$$

Plant A: $10d + 5f \geq 1000$

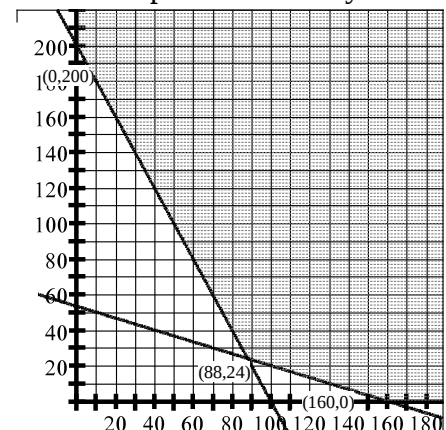
Plant B: $5d + 15f \geq 800$

Cost:

$$C(x, y) = 30d + 35f$$

Answer: 88 hours on dump truck
and 24 hours on fire engine
Minimum cost is \$3480

	Dump hrs (d)	Fire hrs (f)	Combined
Plant A:	10	5	1000
Plant B:	5	15	800
\$:	\$30	\$35	



4. A diet is to include at least 140 milligrams of Vitamin A and at least 145 milligrams of Vitamin B. These requirements can be obtained from two types of food. Type X contains 10 milligrams of Vitamin A and 20 milligrams of Vitamin B per pound. Type Y contains 30 milligrams of Vitamin A and 15 milligrams of Vitamin B per pound. If type X food costs \$12 per pound and type Y food costs \$8 per pound how many pounds of each type of food should be purchased to satisfy the requirements at the minimum cost?

Constraints:

$$x \geq 0; y \geq 0$$

Vit A: $10x + 30y \geq 140$

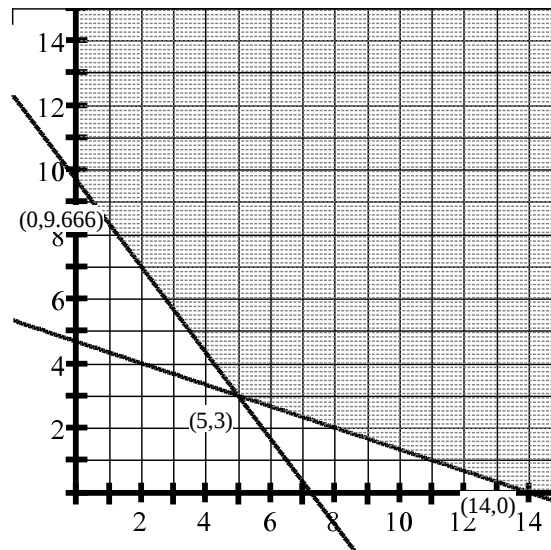
Vit. B: $20x + 15y \geq 145$

Cost:

$$C(x, y) = 12x + 8y$$

	Food X	Food Y	Combined
Vit A:	10	30	140
Vit B:	20	15	145
\$:	\$12	\$8	

Answer: $9\frac{2}{3}$ pounds of type Y food



5. The Cruiser Bicycle Company makes two styles of bicycles: the Traveler, which sells for \$300, and the Tourister, which sells \$600. Each bicycle has the same frame and tires, but the assembly and painting time required for the Traveler is only 1 hour, while it is 3 hours for the Tourister. There are 300 frames and 360 hours of labor available for production. How many bicycles of each model should be produced to maximize revenue?

Traveler = x

Tourister = y

Frame:

Labor:

\$:

Traveler (x)	Tourister (y)	Combined
		300
1	3	360
\$300	\$600	

Constraints:

$$x \geq 0; y \geq 0$$

Frames: $x + y \leq 300$

Labor: $x + 3y \leq 360$

Revenue:

$$R(x, y) = 300x + 600y$$

Answer: 270 Traveler Bikes and 30 Tourester Bikes

