# 4-3:MODELING WITH QUADRATIC FUNCTIONS 

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Algebra 2

A parabola contains points $(0,0),(-1,1)$ and $(1,5)$. What is the equation of this parabola in standard form?

## Draw the rectangular number next in the series:

1. The following pictures illustrate the first five numbers in a sequence we shall call the "rectangular numbers."


Find the next two rectangular numbers:

|  |  |  |  | $4 \times 5$ | $5 \times 6$ | $6 \times 7$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $1 \times 2$ | $2 \times 3$ | $3 \times 4$ |  | $\because: \bullet: ~$ | $\because \bullet: \bullet$ |
|  |  |  | - •• | $\because \bullet$ - |  | $\because \because:$ |
|  | - - | $\because:$ | $\because:$ |  | $\bullet \bullet \bullet$ •* | $\because: 0$ |
| \# of Dots | 2 | 6 | 12 | 20 | 30 | - ${ }^{\text {- }}$ |
|  |  |  |  |  |  |  |
| Term \# | 1 | 2 | 3 | 4 | 5 | 6 |
|  |  | $7 \times 8$ | $8 \times 9$ |  |  |  |
| \# of Dots |  | 56 | 72 |  |  |  |

## Complete the table for the values given and graph the data:

| Term <br> Number | Total dots |
| :---: | :---: |
| 1 | 2 |
| 2 | 6 |
| 3 | 12 |
| 4 | 20 |
| 5 | 30 |

1) What equation does the graph suggest? A Quadratic (parabola)

2) Plot the data in your calculator.

Press: STAT>EDIT>L ${ }_{1}$
Enter the data under Term Number. The equation is of the form:
3) Use the arrow keys to move through
$y=a x^{2}+b x+c$ to $\mathbf{L}_{\mathbf{2}}$ Enter the data you found under Total Dots.
$a=\frac{1}{2}$
$b=\frac{1}{0}$
$c=0$ your hand made graph?
5) Calculate the equation of the line of

Final equation:

$$
x^{2}+x
$$ best fit:

Press: STAT>CALC>\#5 QuadReg
6) Choose the Lists that your data is stored under. (Ex. $\mathrm{L}_{1}, \mathrm{~L}_{2}$ ) Press: Enter
7)Enter the equation of the line under $Y=$

$$
x^{2}+x
$$

8)Graph the equation. Does it fit the data?

Yes, the parabola graphed goes through the points.
9) Use your equation to calculate the $100^{\text {th }}$ term in the series.

$$
x^{2}+x=100^{2}+100=10,100
$$

## 4-5: QUADRATIC EQUATIONS

Algebra 2
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## Ways to Solve Quadratic Equations

1. Solve by Factoring

- Set the equation equal to 0 and factor

2. Solve with Tables

- Enter the equation into $\mathrm{Y}=$
- Create a Table and look for $x$ value when $y=0$

3. Solve by Graphing

- Enter equation into $\mathrm{Y}=$
- Graph equation and use zero function to find $x$ value when $y=$ 0 .


## Solve by Factoring

What are the solutions of the quadratic equation
$x^{2}+3 x-18=0$

$$
\begin{aligned}
& x^{2}+3 x-18=0 \\
& (x+6)(x-3)=0 \\
& x+6=0 \\
& x=-6 \\
& x-3=0 \\
& x=3
\end{aligned}
$$

The solutions to $x^{2}+3 x-18=0$ are $(-6,0)$ and $(3,0)$

## Solve Using a Table

What are the solutions of the quadratic equation $10 x^{2}+2 x-46=x-4$

Enter the quadratic equation $10 x^{2}+x-42=0$ into the calculator and create a table.

Find the $x$ values which have a $y$ value of 0 .

The solutions to $10 x^{2}+2 x-46=x-4$
are $(2,0)$ and $(-2.1,0)$

## Solve by Graphing

What are the solutions of the quadratic equation $5 x^{2}-8=18 x$

$$
\begin{aligned}
5 x^{2}-8 & =18 x \\
5 x^{2}-18 x-8 & =0
\end{aligned}
$$

Enter the quadratic equation $5 x^{2}-18 x-8=0$ into the calculator and graph it.

Use the zero function to find the $x$ values which have a $y$ value of 0 .

The solutions to $5 x^{2}-18 x-8=0$ are $(-0.4,0)$ and $(4,0)$

## Solve by Graphing

What are the solutions of the quadratic equation $5 x^{2}-8=18 x$

Enter the quadratic equation $5 x^{2}-8$ into the calculator as $Y_{1}$ and $18 x$ into the calculator as $Y_{2}$ and graph them.

Use the Intersect function to find the $x$ values where the lines intersect.

The solutions to $5 x^{2}-8=18 x$ are $(-0.4,0)$ and $(4,0)$

The function $f(x)=-0.002 x^{2}+0.77 x$ models the path of a baseball, where $f(x)$ gives the height of the ball and $x$ gives the distance from where it is hit in feet.
a. How far does the ball travel before hitting the ground?

## 385 feet

b. How high does the ball go?

## about 74 feet

c. What is a reasonable domain and range for such a function?

$$
\text { Domain }=[0,400] \text { and Range }=[0,100]
$$

