

Function: The Identity Function

$$f(x) = x$$

Domain:  $(-\infty, \infty)$

Range:  $(-\infty, \infty)$

Inc./Dec./Cons.:  $(-\infty, \infty)$  Always Increasing

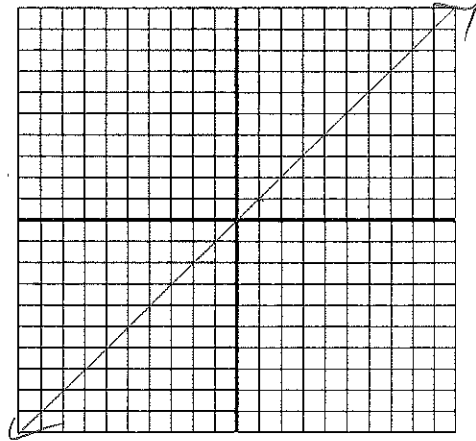
Pos./Neg./Zero:  $(0, \infty)$   $(-\infty, 0)$   $x=0$

Bnd: None

Extr: None

EB:  $\lim_{x \rightarrow -\infty} f(x) = -\infty$   $\lim_{x \rightarrow \infty} f(x) = \infty$

Graph:



Continuity: Continuous  $(-\infty, \infty)$

Sym: Odd function origin

Asymp: None

Function: The Squaring Function

$$f(x) = x^2$$

Domain:  $(-\infty, \infty)$

Range:  $[0, \infty)$

Inc./Dec./Cons.: Dec.  $(-\infty, 0)$  Inc.  $(0, \infty)$

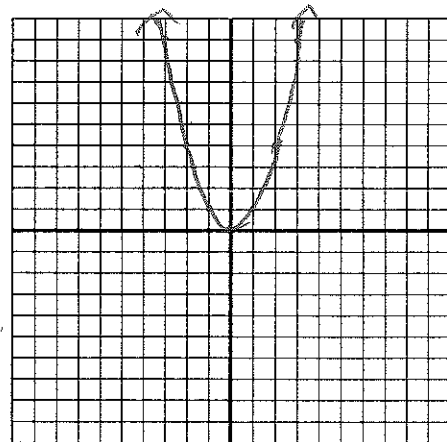
Pos./Neg./Zero:  $(-\infty, 0)$   $(0, \infty)$   $x=0$

Bnd: Below by  $y=0$

Extr: Abs. Min.  $y=0$  @  $x=0$

EB:  $\lim_{x \rightarrow -\infty} f(x) = \infty$   $\lim_{x \rightarrow \infty} f(x) = \infty$

Graph:



Continuity: Continuous  $(-\infty, \infty)$

Sym: Even function

Asymp: None

Function: The Cubing Function  
 $y = x^3$

Domain:  $(-\infty, \infty)$

Range:  $(-\infty, \infty)$

Inc./Dec./Cons.:  $(-\infty, \infty)$  Increasing

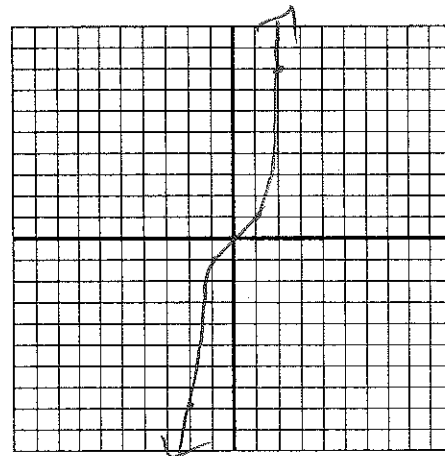
Pos./Neg./Zero:  $(-\infty, 0)$ ,  $(0, \infty)$   $x=0$

Bnd: No Bound

Extr: No Extrema

EB:  $\lim_{x \rightarrow -\infty} f(x) = -\infty$   $\lim_{x \rightarrow \infty} f(x) = \infty$

Graph:



Continuity: Continuous  $(-\infty, \infty)$

Sym: Odd Function origin

Asymp: None

Function: The Reciprocal Function  
 $f(x) = \frac{1}{x}$

Domain:  $(-\infty, 0) \cup (0, \infty)$

Range:  $(-\infty, 0) \cup (0, \infty)$

Inc./Dec./Cons.: Decreasing  $(-\infty, 0)$ ,  $(0, \infty)$

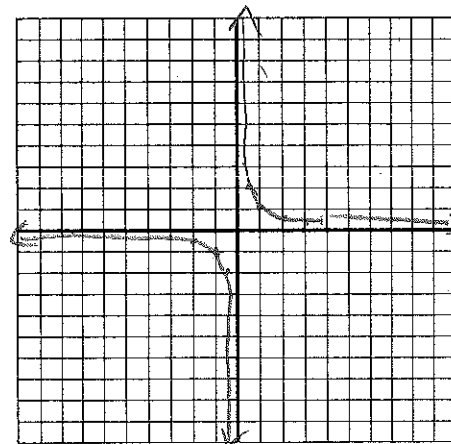
Pos./Neg./Zero:  $(-\infty, 0)$ ,  $(0, \infty)$

Bnd: Not Bounded

Extr: No Extrema

EB:  $\lim_{x \rightarrow -\infty} f(x) = 0$   $\lim_{x \rightarrow \infty} f(x) = 0$

Graph:



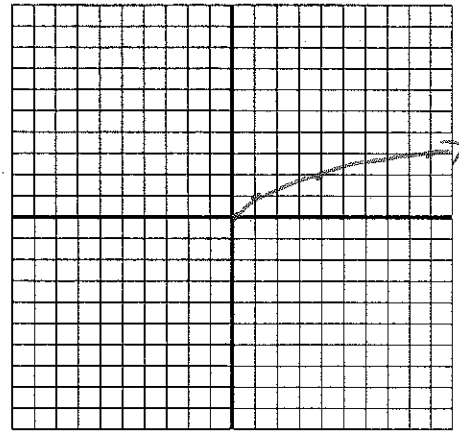
$(-\infty, 0) \cup (0, \infty)$   
Continuity: VA @  $x=0$

Sym: odd function origin

Asymp: VA @  $x=0$  HA @  $y=0$

Function: The Square Root Function  
 $f(x) = \sqrt{x}$

Graph:



Domain:  $[0, \infty)$

Range:  $[0, \infty)$

Inc./Dec./Cons.:  $(0, \infty)$  Increasing

Pos./Neg./Zero:  $(0, \infty)$   $x=0$

Continuity: Continuous  $[0, \infty)$

Bnd: Lower Bound @  $y=0$

Sym: Not Symmetric

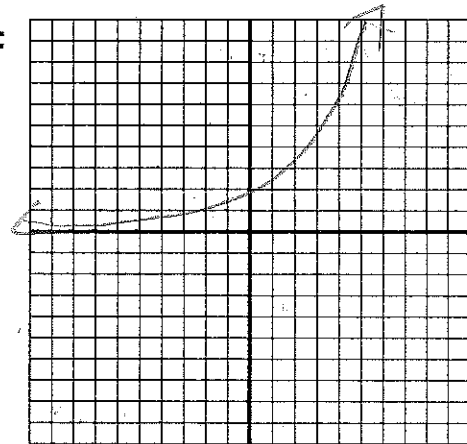
Extr: Abs Min @  $y=0$  @  $x=0$

Asymp: No Asym.

EB:  $\lim_{x \rightarrow \infty} f(x) = \infty$

Function: Exponential  
 $y = e^x$

Graph:



Domain:  $(-\infty, \infty)$

Range:  $(0, \infty)$

Inc./Dec./Cons.: I!  $(-\infty, \infty)$

Continuity: Continuous  $(-\infty, \infty)$

Bnd: Lower bound  $y=0$

Sym: Not Symmetric

Extr: No Extrema

Asymp:  $y=0$

EB:  $\lim_{x \rightarrow -\infty} f(x) = 0$        $\lim_{x \rightarrow \infty} f(x) = \infty$

Function: The Natural Log Function  
 $f(x) = \ln(x)$

Domain:  $(0, \infty)$

Range:  $(-\infty, \infty)$

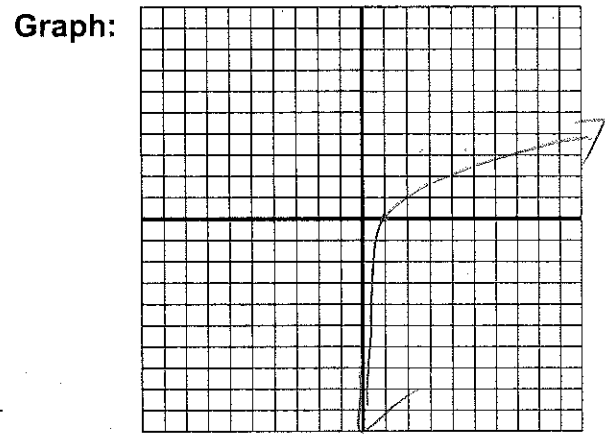
Inc./Dec./Cons.: I:  $(0, \infty)$

Pos./Neg./Zero:  $(0, 1)$   $(1, \infty)$  Z:  $x=1$

Bnd: No Bound

Extr: No Extrema

EB:  $\lim_{x \rightarrow \infty} f(x) = \infty$



Continuity: Continuous  $(0, \infty)$

Sym: Not Symmetric

Asymp: VA @  $x=0$

Function: The Sine Function  
 $f(x) = \sin x$

Domain:  $(-\infty, \infty)$

Range:  $[-1, 1]$   
 $D: ((4n+1)\frac{\pi}{2}, (4n+3)\frac{\pi}{2})$

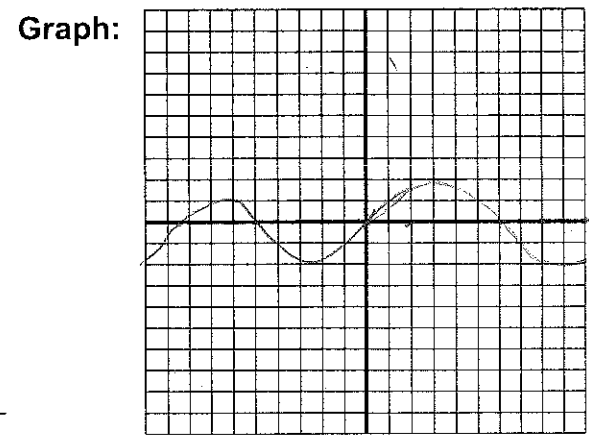
Inc./Dec./Cons.: I:  $((4n-1)\frac{\pi}{2}, (4n+1)\frac{\pi}{2})$   
Z:  $\pi n$

Pos./Neg./Zero: P:  $(2\pi n, (2n+1)\pi)$  N:  $((2n+1)\pi, (4n+1)\pi)$

Bnd: LB:  $y=-1$  UB:  $y=1$

Extr: Abs. Max @  $\frac{\pi}{2}(4n+1)$  Abs. Min @  $\frac{\pi}{2}(4n+1)$

EB:  $\lim_{x \rightarrow \pm\infty} f(x)$  oscillates between  $-1$  &  $1$



Continuity: Continuous  $(-\infty, \infty)$

Sym: odd function origin

Asymp: none

Function: The Cosine Function  
 $f(x) = \cos x$

Domain:  $(-\infty, \infty)$

Range:  $[-1, 1]$

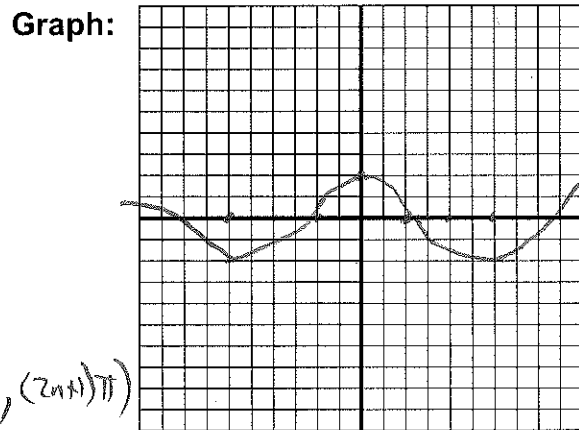
Inc./Dec./Cons.: I:  $((2n-1)\pi, 2n\pi)$  D:  $(2n\pi, (2n+1)\pi)$   
N:  $(4n+1)\frac{\pi}{2}, (4n+3)\frac{\pi}{2}$

Pos./Neg./Zero: A:  $(4n-1)\frac{\pi}{2}, (4n+1)\frac{\pi}{2}$  Z:  $\frac{\pi}{2}(2n+1)$  Continuity: Continuous  $(-\infty, \infty)$

Bnd: Above:  $y=1$  Below:  $y=-1$   
Abs min @  $y=-1$  @  $x=\pi(2n+1)$

Extr: Abs Max @  $y=1$  @  $x=2n\pi$

EB:  $\lim_{x \rightarrow \pm\infty} f(x)$ : oscillates between  $y=-1$  &  $y=1$



Sym: Even Function  $y$ -axis

Asymp: None

Function: The Absolute Value Function  
 $f = |x|$

Domain:  $(-\infty, \infty)$

Range:  $[0, \infty)$

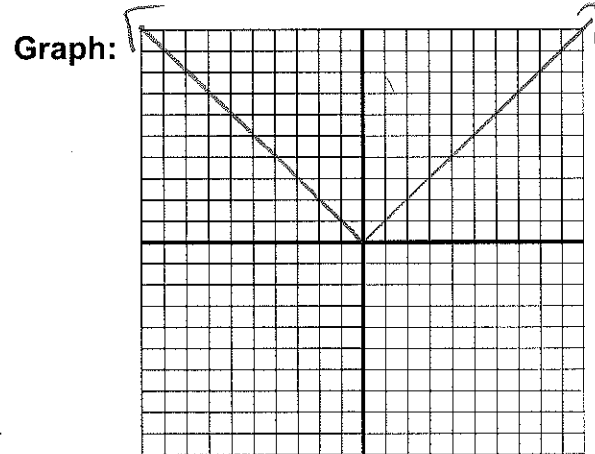
Inc./Dec./Cons.: I:  $(0, \infty)$  D:  $(-\infty, 0)$   
Z: @  $x=0$

Pos./Neg./Zero: A:  $(-\infty, 0) \cup (0, \infty)$

Bnd: lower bound @  $y=0$

Extr: Abs min  $y=0$  @  $x=0$

EB:  $\lim_{x \rightarrow -\infty} f(x) = \infty$   $\lim_{x \rightarrow \infty} f(x) = \infty$



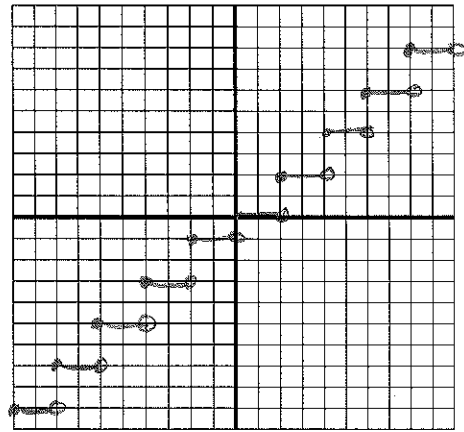
Continuity: Continuous  $(-\infty, \infty)$

Sym: Even  $y$ -axis

Asymp: None

Function: The Greatest Integer Function  
 $f(x) = \lfloor x \rfloor$

Graph:



Domain:  $(-\infty, \infty)$

Range: All integers

Inc./Dec./Cons.: Constant on  $(-\infty, \infty)$

Pos./Neg./Zero: P:  $[1, \infty)$  N:  $(-\infty, -1)$  Z:  $[0, 1)$  Continuity: Discontinuity @ each integer

Bnd: None

Sym: Neither

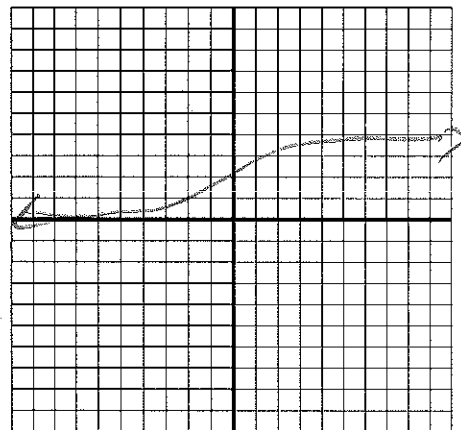
Extr: None

Asymp: None

EB:  $\lim_{x \rightarrow -\infty} f(x) = -\infty$   $\lim_{x \rightarrow \infty} f(x) = \infty$

Function: The Logistic Function  
 $f(x) = \frac{1}{1+e^{-x}}$

Graph:



Domain:  $(-\infty, \infty)$

Range:  $(0, 1)$

Inc./Dec./Cons.: I:  $(-\infty, \infty)$

Pos./Neg./Zero: P:  $(-\infty, \infty)$

Continuity: Continuous  $(-\infty, \infty)$

Bnd: Below @  $y=0$  Above @  $y=1$

Sym: None

Extr: None

Asymp: HA @  $y=0, y=1$

EB:  $\lim_{x \rightarrow -\infty} f(x) = 0$   $\lim_{x \rightarrow \infty} f(x) = 1$