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## Allgebrara III Advancedl andl $\mathbb{C P}$ Summer Packet

Algebra II Advanced and CP are very rigorous and fast-paced courses. In order to prepare for the rigor of this course, you will need to be familiar with the topics in this packet prior to starting the school year. Teachers will not spend a large amount of time reviewing these topics.

This packet is due on the first day of school. This packet will only be graded for completion. If you are unsure of how to answer some of the questions in the packet, please see your Algebra II teacher for extra help during the first week of school.

## Prerequisite Skills for Algebra II

1) Simplify and evaluate expressions
2) Solve basic equations (linear and quadratic)
3) Solve absolute value equations
4) Determine if relations are functions or not
5) Function notation
6) Domain and range of a function
7) Calculate/Interpret the equation of a line
8) Graph linear functions
9) Solve systems of 2 equations
10) Solve and graph inequalities
11) Simplify and factor polynomial expressions
12) Simplify radical expressions
13) Solve and write explanations for word problems

Skill \#1: Simplify and Evaluate Algebraic Expressions
Simplify the expressions by combining like terms.

1. $5 a-a$
2. $-(3 x-4 y)+2(2 y-6 x)$
3. $7 b-(3 a-8 b)$
4. $-a^{2}+b^{2}-\frac{a^{2}}{2}$
5. $0.5 x-1.5 x$
6. $\left(\frac{r}{2}\right)^{2}+3 r^{2}+r$

Evaluate the expressions for the given value of the variable.
7. $x+2 x-x-1 ; x=2$
8. $5 c^{3}-6 c^{2} ; c=-5$
9. $y^{2}+4 ; y=\sqrt{7}$
10. $4 a+7 b-3+6 b$;
11. $12(1.1)^{t} ; t=8$
12. $\frac{3 k+2(k-4)}{k+8} ; k=-3$
12. Write an expression to model the situation:

You have a summer job at a car wash. You earn $\$ 8.50$ per hour and are expected to pay a one-time fee of $\$ 15$ for the uniform. If you work $x$ hours in your first week, how much money will you make in that week?

Solve each equation.
13. $5 c-9=8-2 c$
14. $5(2-g)=0$
15. $6(n-4)=3 n$
16. $x^{2}=16$
17. $3 x^{2}-5=22$
18. $\sqrt{x}+3=8$
19. The first stage of a rocket burns for 28 seconds longer than the second stage. If the rocket's total burning time is 158 seconds, for how long does each stage burn?
20. The length of a rectangle is 3 cm greater than the width. The perimeter is 24 cm . What are the dimensions of the rectangle?

Solve each formula for the indicated variable.
21. $v=s^{2}+\frac{1}{2} s h$; for $h$
22. $C=\frac{5}{9}(F-32)$; for $F$.

Skill \#3: Solve Absolute Value Equations
Solve each equation. Check for extraneous solutions.
23. $|2 x+8|-4=12$
24. $|3 x-2|=7$
25. $|x-1|=5 x+10$
26. $|2 x+5|=3 x+4$

## Skill \#4: Relations and Functions

Determine if each relation is a function.
27. $\{(2,4),(3,5),(2,7),(1,8)\}$
28. $\{(1,3),(2,3),(3,3)\}$
29.

30.


Find $f(-4)$ for each function.
31. $f(x)=2 x^{2}+3 x-7$
32. $f(x)=\frac{2}{x}$
33. $f(t)=t^{3}-\frac{t}{2}$

Solve for the missing variable.
34. What value of $x$ makes $f(x)=8$ if $f(x)=3 x+12$ ?
35. What value(s) of $t$ make $f(t)=2$, if $f(t)=t^{2}-7$.

## Evaluate the function.

36. If $f(x)=2 x+3$, what is the function for $f(x+2)$ ?
37. If $f(x)=2 x+3$, what is the function for $f(2 x)$ ?

## Identify the domain and range of each relation.

38. $\{(2,4),(3,5),(2,7),(1,8)\}$

Domain: $\qquad$
Range: $\qquad$
40.


Domain: $\qquad$
Range: $\qquad$
42.


Domain: $\qquad$
Range: $\qquad$
39. $\{(1,3),(2,3),(3,3)\}$

Domain: $\qquad$
Range: $\qquad$
41.


Domain: $\qquad$
Range: $\qquad$
43.


Domain: $\qquad$
Range: $\qquad$
44. Identify the slope and the $y$-intercept of the following linear equations.
a. $y=\frac{1}{3} x+9$
b. $y=-2 x$
c. $2 x-4 y=12$
d. $3 x+4 y=18$
45. Find the equation in slope-intercept form of a line with a slope of -2 and a $y$-intercept of -9 .
46. Find the equation of a line in slope-intercept form that has a slope of 4 and passes through $(3,8)$.
47. Find the equation of a line in slope-intercept form that passes through $(2,5)$ and $(-2,3)$.
48. Convert the equation into standard form: $\quad y=\frac{1}{3} x+7$

Skill \#8: Graphing Linear Functions
Graph the following linear functions on the coordinate plane.
49. $f(x)=3 x+2$

51. $3 x+4 y=12$

50. $f(x)=-\frac{2}{5} x-1$

52. $2 x-5 y=15$


Skill \#9: Solving Systems of 2 Equations
Solve the systems by substitution. Write your answer as a coordinate pair(s), if it exists.
53. $\left\{\begin{array}{c}y=6 x-11 \\ -2 x-3 y=-7\end{array}\right.$
54. $\left\{\begin{array}{c}y=4 x-9 \\ y=x-3\end{array}\right.$
55. $\left\{\begin{array}{l}y=-2 x+6 \\ 2 x+y=-7\end{array}\right.$

Solve the systems by elimination. Write your answer as a coordinate pair, if it exists.
56. $\left\{\begin{array}{c}6 x-12 y=24 \\ -x-6 y=4\end{array}\right.$
57. $\left\{\begin{aligned} 3 x-4 y & =2 \\ -6 x+8 y & =-4\end{aligned}\right.$
58. $\left\{\begin{array}{c}-11 x-4 y=36 \\ -10 x-10 y=20\end{array}\right.$

Solve the systems by graphing. Write your answer as a coordinate pair, if it exists.
59. $\left\{\begin{array}{c}y=x+2 \\ x=-3\end{array}\right.$

60. $\left\{\begin{array}{c}y=-3 x+4 \\ 3 x-y=2\end{array}\right.$


Skill \#10: Solve and Graph Inequalities
Solve each inequality. Then, graph it on the number line. Label the number line for each problem.
61. $7 x+4>18$
62. $-2(x+5) \geq-16$

63. $y<-2 x+7$

64. $2 x+6 y \geq 18$


Skill \#11: Simplify and Factor Polynomial Expressions
Simplify the expressions by multiplying and combining like terms.
65. $(2 x+7)(3 x-5)$
66. $2 x^{2}\left(x^{3}+5 x^{2}-6\right)$
67. $(3 x-1)\left(x^{2}+4 x-2\right)$
68. $\left(x^{2}-3 x+4\right)\left(x^{2}+x-5\right)$

Factor the given expressions using the method described.
69. Factor out the greatest common factor:
a. $10 x^{2} y^{2}+15 x y^{3}-5 x y^{2}$
b. $-6 r s-12 r^{2} s+9 r t$
70. Factor by difference of squares. If the expression is not factorable, write "N.F."
a. $x^{2}-81$
b. $4 t^{2}-25$
c. $z^{2}+36$
d. $x^{4}-49$
71. Factor the trinomial into two binomials. If the expression is not factorable, write "N.F."
a. $x^{2}+x-12$
b. $x^{2}+13 x+40$
c. $x^{2}-17 x+72$
d. $2 x^{2}-6 x-8$
e. $2 x^{2}-9 x-18$
f. $12 x^{2}+11 x-5$
72. $2 \sqrt{3}+5 \sqrt{3}$
73. $2 \sqrt{5} \times 3 \sqrt{5}$
74. $3 \sqrt{3} \times 4 \sqrt{5}$

Simplify the radicals:
75. $\sqrt{25}$
76. $\sqrt{200}$
77. $\sqrt{96}$
78. $\sqrt{216}$
79. $\sqrt{80 x^{2}}$
80. $\sqrt{125 x^{3}}$

## Skill \#13: Word Problems

81. Phil and Matt made cookies for a fundraiser at their school. Phil made $25 \%$ more cookies than Matt. The cookies sold for $\$ 0.25$ each. After the sale, $20 \%$ of the combined total cookies remained.
a. Create an equation to represent the total amount of money Matt and Phil will earn at the fundraiser based on the number of cookies Matt baked. Explain how you determined your equation.
b. Phil and Matt made a total of $\$ 72.00$ at the fundraiser. How many cookies did Phil make, and how many did Matt make? Show your work.
c. Next month, Matt and Phil plan to bake the same number of cookies again, but want to sell them for $\$ 0.50$ each. They estimate they will only sell $70 \%$ of the cookies because of the price increase. Based on their prediction, should they increase the price? Justify your answer.
82. Let $|x|+|y|=c$, where $c$ is a real number.

Determine the number of solutions for $x$ and $y$ for each of the following scenarios. Justify your answer for each case.

Case 1: $c<0$
Case 2: $c=0$
Case 3: $c>0$

